

In[95]:= (* BENEFITS OF SHARING INFORMATION IN ITERATIVE LEARNING CONTROL,
Case of Pure Process Noise, Angela Schöllig, Oct 2009 *)

In[96]:= Remove["Global`*"]

In[97]:= $pN = (a + b + j b (n a + b)) / ((1 + j (n a + b)) (1 + j b))$

$$\text{Out[97]} = \frac{a + b + b j (b + a n)}{(1 + b j) (1 + j (b + a n))}$$

In[98]:= $p11 = \text{Simplify}[pN /. n \rightarrow 1]$

$$\text{Out[98]} = \frac{a + b}{1 + a j + b j}$$

In[99]:= $Rproc = \text{Simplify}[(1 + p11) / (1 + pN)]$

$$\text{Out[99]} = \frac{1 + \frac{a+b}{1+a j+b j}}{1 + \frac{a+b+b j (b+a n)}{(1+b j) (1+b j+a j n)}}$$

In[100]:= $\text{FullSimplify}[D[Rproc, n]]$

$$\text{Out[100]} = \frac{a^2 j (1 + b j) (1 + a + b + (a + b) j)}{(1 + (a + b) j) (a + (1 + b j) (1 + b + b j) + a j (1 + b + b j) n)^2}$$

In[101]:= $RprocN = \text{FullSimplify}[\text{Limit}[Rproc, n \rightarrow \text{Infinity}]]$

$$\text{Out[101]} = \frac{(1 + b j) (1 + a + b + (a + b) j)}{(1 + b + b j) (1 + (a + b) j)}$$

In[102]:= $\text{FullSimplify}[D[RprocN, a]]$

$$\text{Out[102]} = \frac{1 + b j}{(1 + b + b j) (1 + (a + b) j)^2}$$

In[103]:= $RprocNa = \text{FullSimplify}[\text{Limit}[RprocN, a \rightarrow \text{Infinity}]]$

$$\text{Out[103]} = \frac{(1 + j) (1 + b j)}{j (1 + b + b j)}$$

In[104]:= $\text{FullSimplify}[D[RprocNa, b]]$

$$\text{Out[104]} = -\frac{1 + j}{j (1 + b + b j)^2}$$

In[105]:= $RprocNab = \text{FullSimplify}[\text{Limit}[RprocNa, b \rightarrow 0]]$

$$\text{Out[105]} = 1 + \frac{1}{j}$$