

In[129]:= (\* BENEFITS OF SHARING INFORMATION IN ITERATIVE LEARNING CONTROL,  
Case of Pure Measurement Noise, Angela Schöellig, Oct 2009 \*)

In[130]:= Remove["Global`\*"]

In[131]:=  $pN = (a + b + j b (n a + b)) / ((1 + j (n a + b)) (1 + j b))$

Out[131]= 
$$\frac{a + b + b j (b + a n)}{(1 + b j) (1 + j (b + a n))}$$

In[132]:=  $p11 = \text{Simplify}[pN /. n \rightarrow 1]$

Out[132]= 
$$\frac{a + b}{1 + a j + b j}$$

In[133]:=  $Rmeas = \text{Simplify}[p11 / pN]$

Out[133]= 
$$\frac{(a + b) (1 + b j) (1 + b j + a j n)}{(1 + a j + b j) (a + b + b j (b + a n))}$$

In[134]:=  $\text{Expand}[\text{Numerator}[Rmeas]]$

Out[134]=  $a + b + 2 a b j + 2 b^2 j + a b^2 j^2 + b^3 j^2 + a^2 j n + a b j n + a^2 b j^2 n + a b^2 j^2 n$

In[135]:=  $\text{Expand}[\text{Denominator}[Rmeas]]$

Out[135]=  $a + b + a^2 j + 2 a b j + 2 b^2 j + a b^2 j^2 + b^3 j^2 + a b j n + a^2 b j^2 n + a b^2 j^2 n$

In[136]:=  $\text{FullSimplify}[D[Rmeas, b]]$

Out[136]= 
$$- \frac{a^2 j (-1 + n) ((1 + b j) (1 + 2 a j + 3 b j) + a j (1 + a j + 2 b j) n)}{(1 + (a + b) j)^2 (a + b + b^2 j + a b j n)^2}$$

In[137]:=  $\text{FullSimplify}[D[Rmeas, a]]$

Out[137]= 
$$\frac{a j (1 + b j) (-1 + n) ((a + 2 b) (1 + b j) + a b j n)}{(1 + (a + b) j)^2 (a + b + b^2 j + a b j n)^2}$$

In[138]:=  $\text{FullSimplify}[D[Rmeas, n]]$

Out[138]= 
$$\frac{a^2 (a + b) j (1 + b j)}{(1 + (a + b) j) (a + b + b^2 j + a b j n)^2}$$

In[139]:=  $Rmeasb = \text{FullSimplify}[\text{Limit}[Rmeas, b \rightarrow 0]]$

Out[139]= 
$$\frac{1 + a j n}{1 + a j}$$

In[140]:=  $\text{FullSimplify}[\text{Limit}[Rmeasb, a \rightarrow \text{Infinity}]]$

Out[140]=  $n$