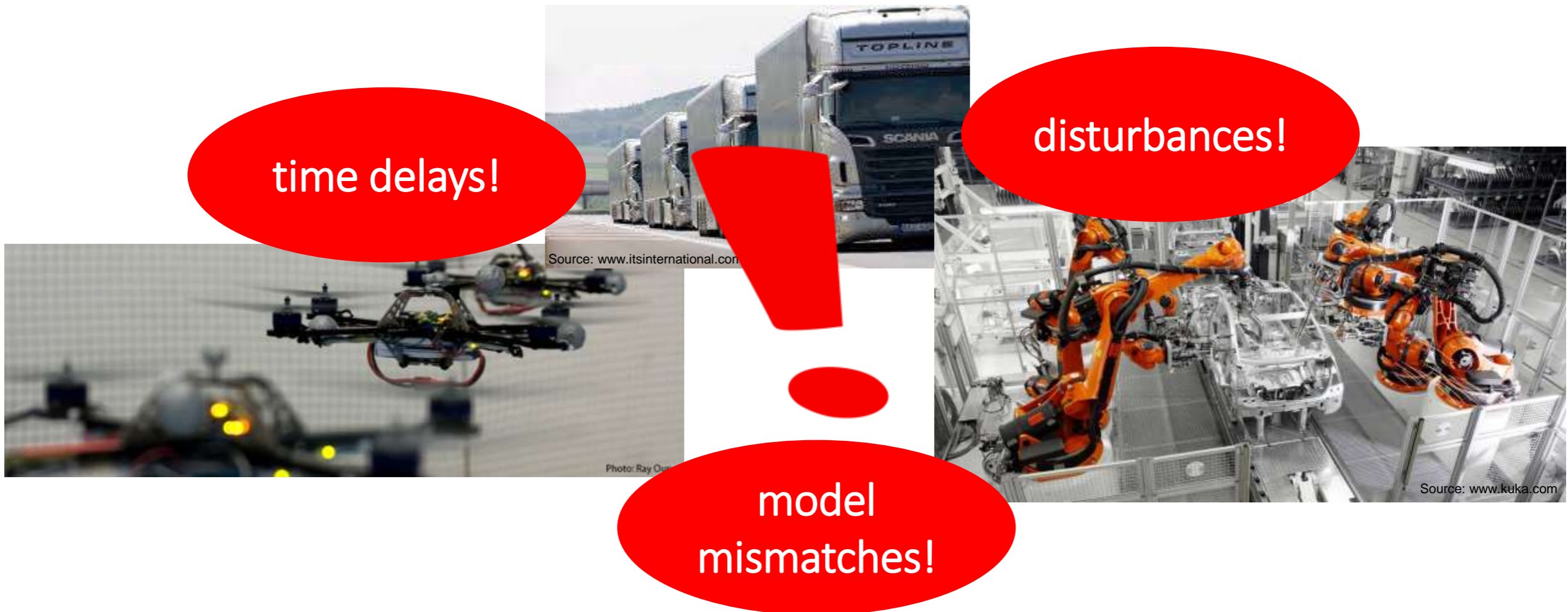


# Distributed Iterative Learning Control for a Team of Quadrotors

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Andreas Hock, Angela P. Schoellig

*13 December 2016*



*Learning can make multi-robot coordination more accurate or faster, and enable it to adapt to changing tasks or environment!*

# Distributed ILC for a Team of Quadrotors

## Distributed Control:

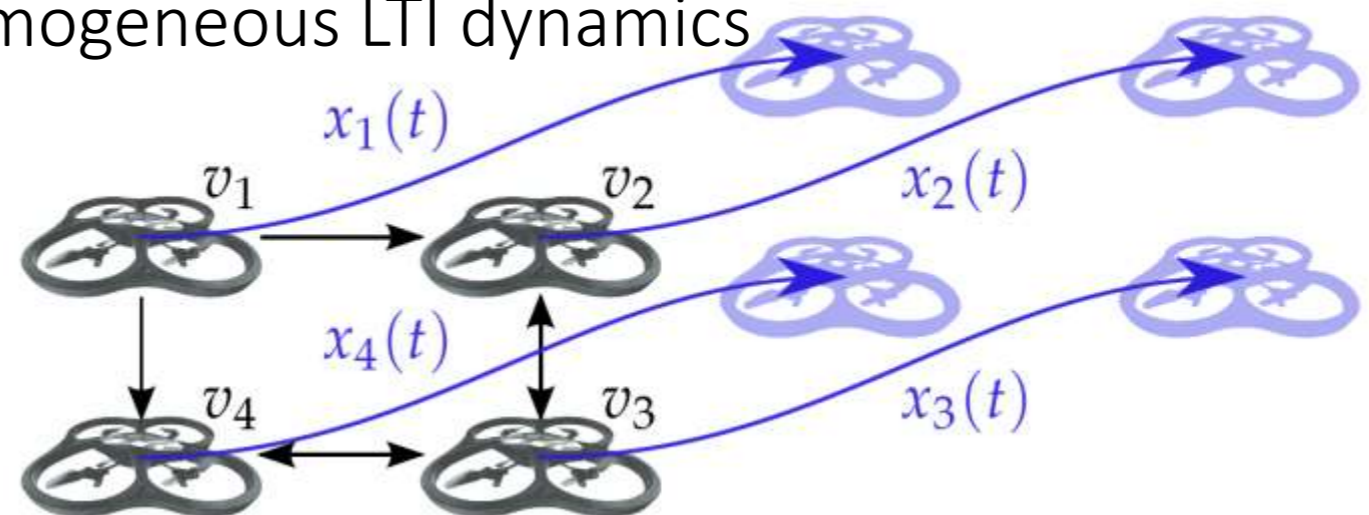
- No central control unit
- Autonomous agents
- Communication only between certain neighbors

## Iterative Learning Control (ILC):

- Machine Learning technique
- Learning by repetition
- Updating the feedforward input based on past measurements

## Team of Quadrotors:

- Goal: synchronous formation flying
- Homogeneous LTI dynamics



## Related Work

There exist several studies on...

- ILC for a **single** agent:
  - theoretic survey [Bristow, 2006]
  - quadrotor vehicle [Schoellig, 2012]
- **multi-agent** ILC: [Ahn, 2009; Meng, 2012; Yang, 2012]

## Open Problems

- previous stability proofs for multi-agent ILC restricted to D-type learning functions
  - => *cannot compensate for position offsets*
- pure feedforward control
  - => *cannot compensate for non-repetitive errors*
- no experimental validation so far

theoretical development of advanced ILC algorithms  
for multi-agent systems (MAS) & experimental implementation

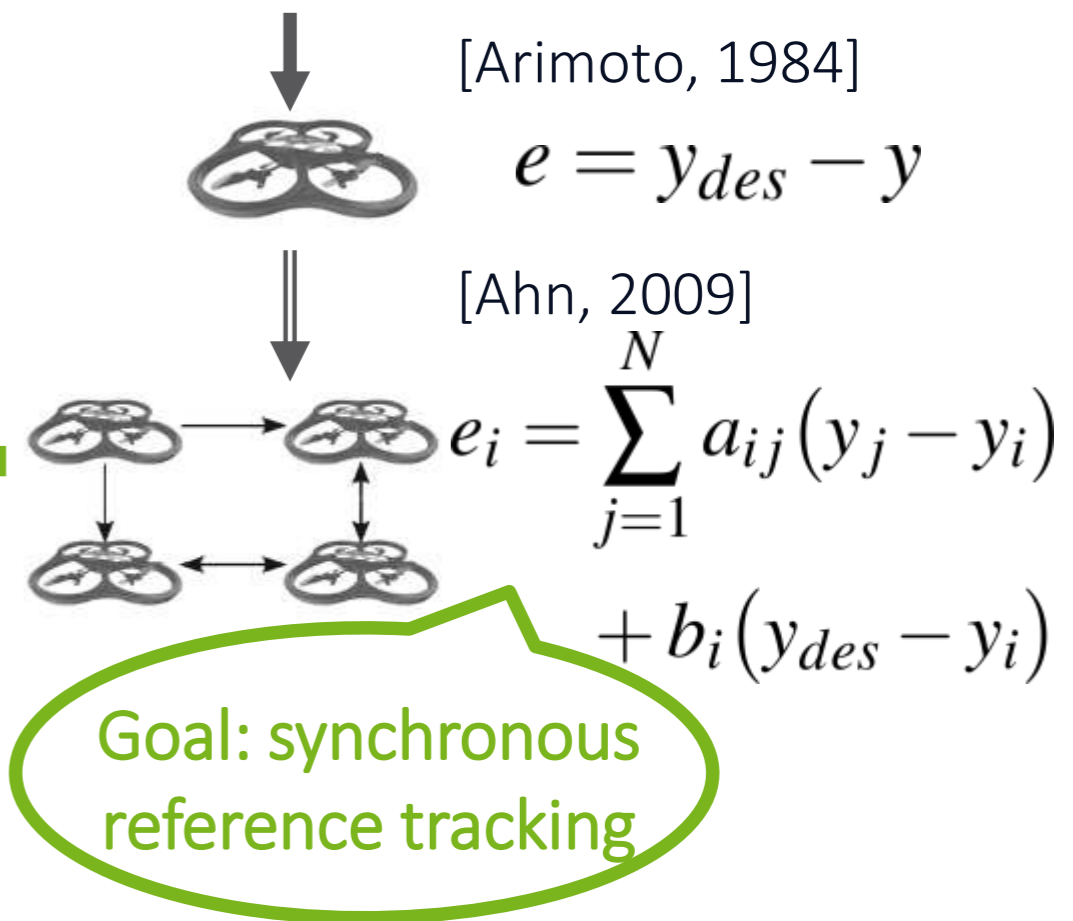
Idea of ILC :

*Use error information to improve feedforward input for subsequent iterations!*

New Input = Old Input + Correcting Action, depending on error in last trial

so far input update for multi-agent ILC only based on error derivative

- ↳ restrictive, limited design parameters
- ↳ position offsets can not be compensated



→  $u_{i,k+1} = u_{i,k} + \mathbf{L} \cdot e_{i,k}$  where  $\mathbf{L}$  can be an arbitrary linear mapping in discrete time!

↑                   ↑  
agent  $i$            iteration  $k$

## Lifted System Representation

[Bristow, 2006]

- ILC stability analysis in discrete time
- time samples  $\Rightarrow$  full trajectory vectors

## Graph Theoretical Definitions

[Yang, 2012]

- Concept of graph Laplacian  $\mathcal{L}_G$
- Reference as virtual leader node  $\Rightarrow \mathcal{B}$
- Single agents' states  $\Rightarrow$  full MAS state

System Dynamics  $\mathbf{P}$ ,  
Learning Function  $\mathbf{L}$ ,  
w/ diagonal entries  
 $p_1, l_0 \in \mathbb{R}$

Graph Information  
 $(\mathcal{L}_G + \mathcal{B})$   
with eigenvalues  
 $\lambda_i$

### Theorem 1:

The multi-agent ILC is **asymptotically stable** if and only if

$$\rho(\mathbf{I} - (\mathcal{L}_G + \mathcal{B}) \otimes \mathbf{L}\mathbf{P}) < 1.$$

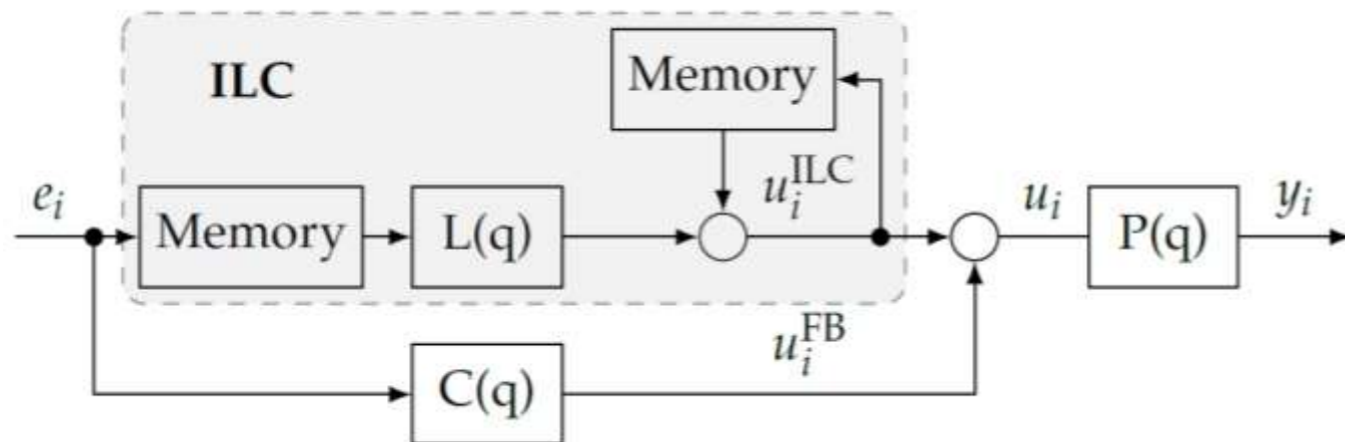
For causal learning, this holds iff

$$\max_i |1 - \lambda_i l_0 p_1| < 1.$$

*crucial design  
parameter*

# Distributed ILC for MAS – Combination with Consensus Feedback Control

## ILC with Feedback



## Theorem 2:

A time domain feedback term

$$u_i^{FB} = C \cdot e_i,$$

with linear mapping  $C$ , does not affect stability of the proposed ILC system!

**NEW!**

COMPARISON	Feedback Control (Consensus)	ILC	ILC + Consensus Feedback
<i>learn from tracking errors</i>	✗	✓	✓
<i>compensate for non-repetitive errors</i>	✓	✗	✓
<i>incorporate repetitive disturbances</i>	✗	✓	✓

[Link to Video](#)



## Distributed Iterative Learning Control for a Team of Two Quadrotors

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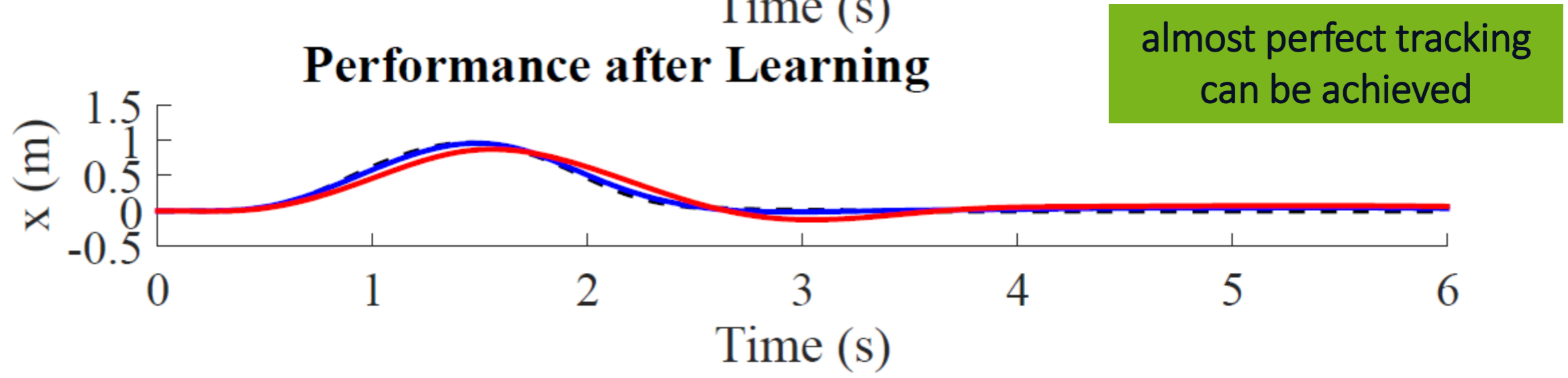
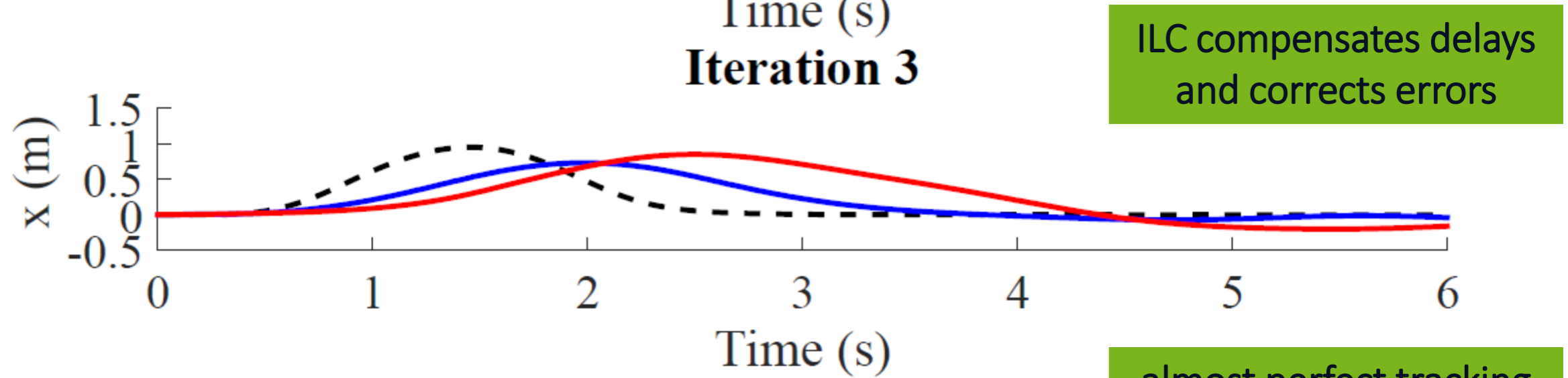
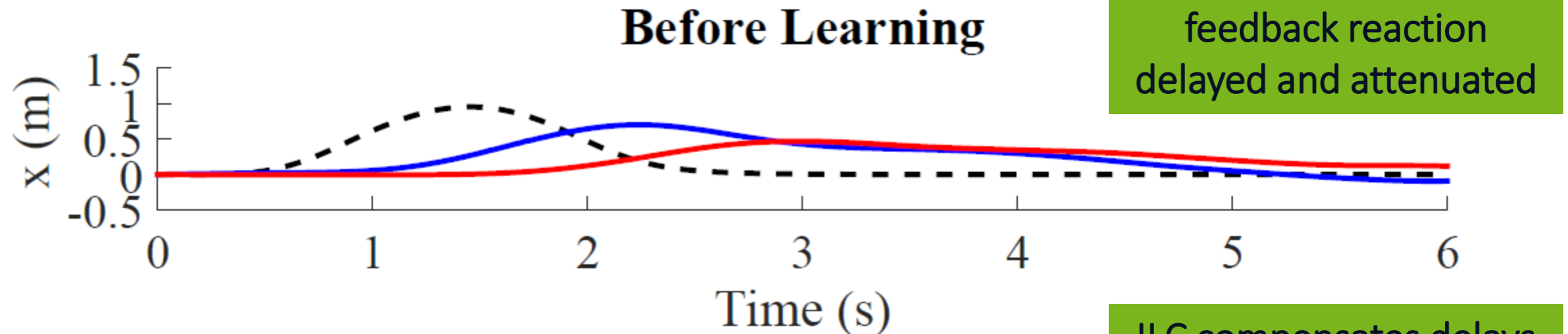
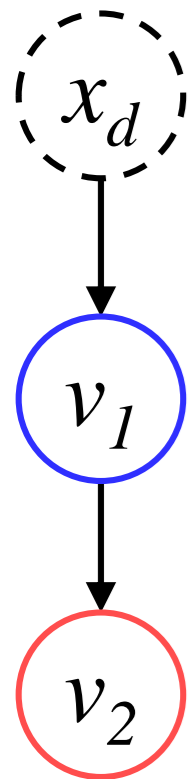
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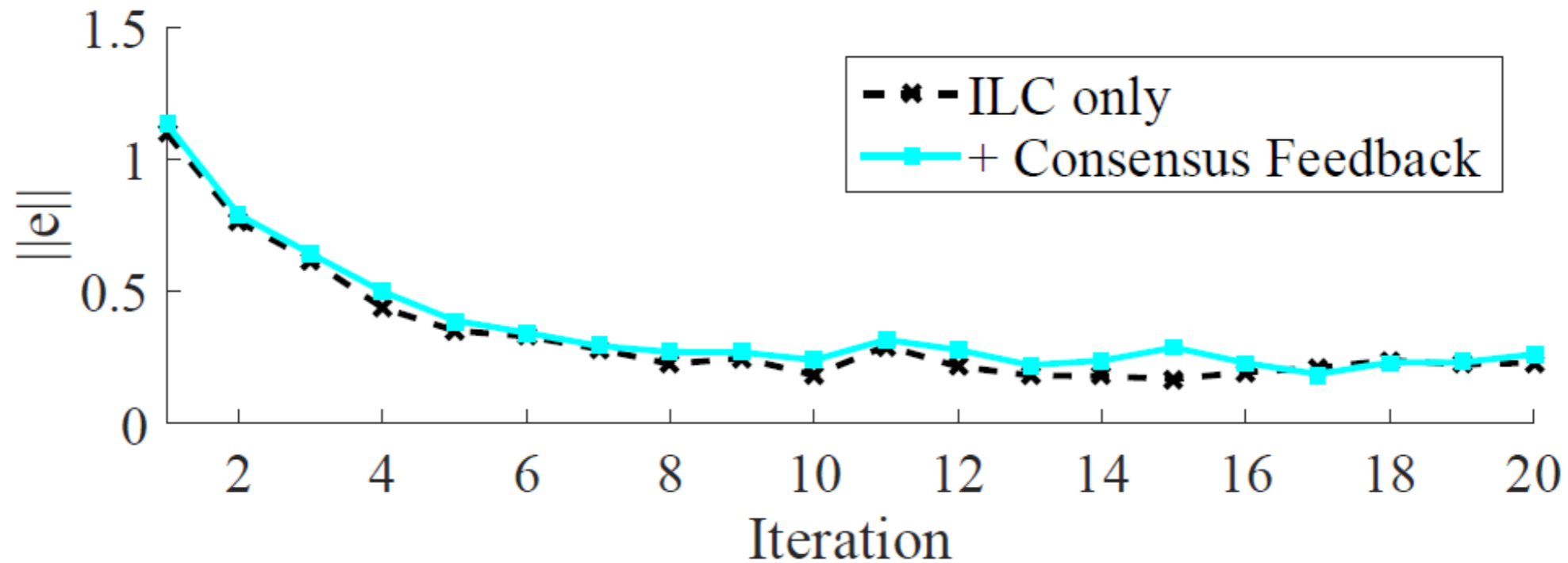


# Experimental Results - *Trajectories in $x$ over time*

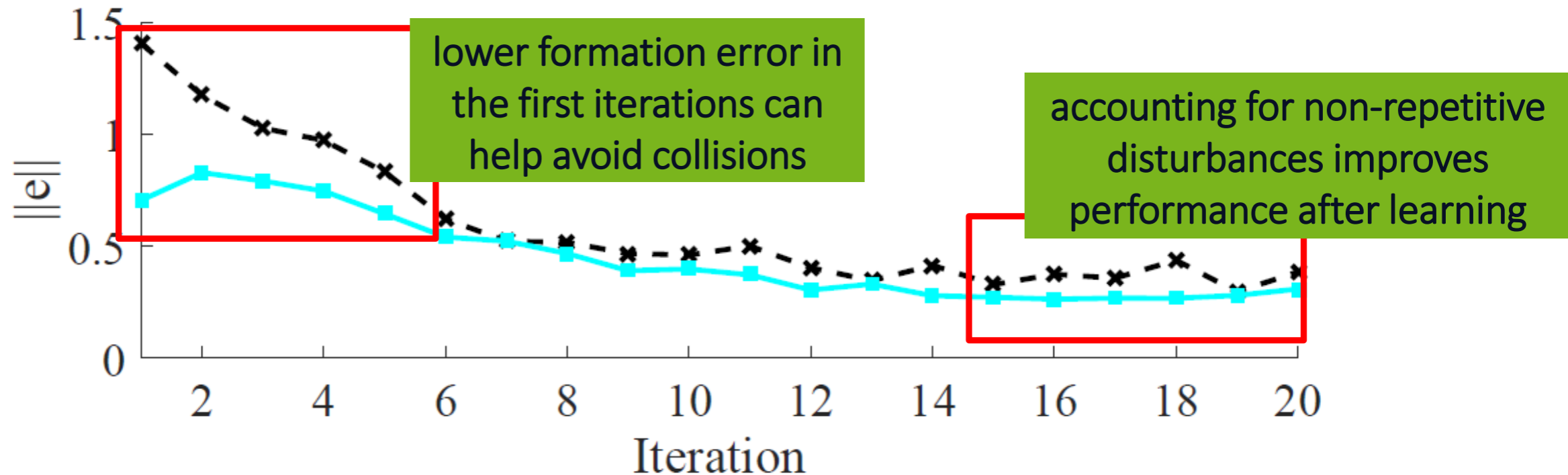


# Experimental Results - Error Convergence Comparison

## Vehicle 1



## Vehicle 2



- ➔ **Generalized stability proof** demonstrated that the multi-agent ILC algorithm converges if  $l_0$  is chosen properly => many tuning options for input-update rule
- ➔ We proved that including a **consensus feedback controller** does not affect stability but improves performance as it compensates for non-repeating disturbances
- ➔ Multi-agent ILC was successfully implemented on a **real experiment** for the first time

# Experimental Results – Experiment with four quadrotors

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[Link to Video](#)



## Distributed Iterative Learning Control for a Team of Four Quadrotors

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- ➔ We proved that including a **consensus feedback controller** does not affect stability but improves performance as it compensates for non-repeating disturbances
- ➔ Multi-agent ILC was successfully implemented on a **real experiment** for the first time

# Thank you!

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