

## Particle Filter for Tracking an Object Moving on a Circle

A particle filter is to be designed for tracking the position of an object  $B$  that is randomly moving on a circle with radius 1. The distance to the object can be measured from a given observation point  $P$  at location  $x = L$ . A schematic drawing is shown in Fig. 1.

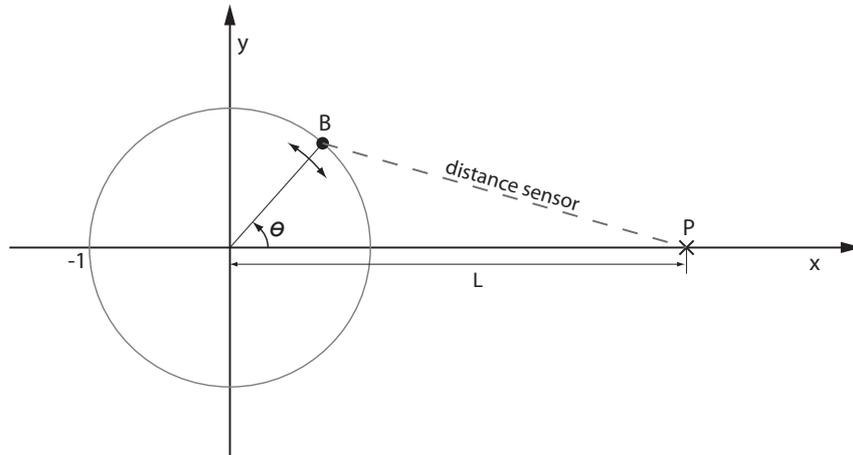


Figure 1: The moving object with relevant physical quantities.

At time  $k$ , the location of the object on the circle is given by  $\theta(k) \in [0, 2\pi)$ . The random motion of the object is described by

$$\theta(k) = \text{mod} (\theta(k-1) + s(k-1) + p, 2\pi), \quad k = 1, 2, \dots,$$

where  $s(k) \in [-\bar{s}, \bar{s}]$  is a uniformly distributed random variable, and the constant unknown bias  $p$  is uniformly distributed on the interval  $[-\bar{s}, \bar{s}]$ .

At varying instances of time, measurements of the distance sensor may be received that are corrupted by sensor noise, i.e.

$$z_1(k) = \left( (L - \cos \theta(k))^2 + (\sin \theta(k))^2 \right)^{\frac{1}{2}} + w(k),$$

with  $w(k) \in [-e, e]$  uniformly distributed. An additional half-plane sensor occasionally provides information about the vertical position of the object,

$$z_2(k) = \begin{cases} 1 & \text{if } \theta(k) \in [0, \pi) \\ -1 & \text{if } \theta(k) \in [\pi, 2\pi). \end{cases}$$

At any instance of time  $k$ , measurements may be available from one, two, or none of the sensors. All random variables  $s(k)$ ,  $p$ , and  $w(k)$  are assumed to be mutually independent and independent over time.

## Objective

The objective is to design a particle filter to estimate the object's location on the circle. The estimator has access to the time  $k$ , and possibly the measurements  $z_1(k)$  and/or  $z_2(k)$ . Furthermore, the total number  $N$  of particles in the filter and the values of all physical constants  $L$ ,  $\bar{s}$ , and  $e$  are known to the estimator. The angle  $\theta(k)$  and the bias  $p$  are estimator states.

## Provided Matlab Files

A set of Matlab files is provided on the class website. Please use them for solving the above problem.

<code>script.m</code>	Matlab script that is used to simulate the truth system, run the estimator, and display the results.
<code>Estimator.m</code>	Matlab function template to be used for your implementation of the particle filter.
<code>PhysicalConstants.m</code>	Physical constants, known to the estimator.
<code>SimulationConstants.m</code>	Sample problem data, <b>not</b> known to the estimator.
<code>Uniform.m</code> ,	Uniform random number generators.
<code>UniformMinMax.m</code>	

## Task

Implement your solution for the particle filter in the file `Estimator.m`. Your code has to run with the Matlab script `script.m` and problem data as for example given in `PhysicalConstants.m` and `SimulationConstants.m`. For your estimator, use the function definition as given in the template `Estimator.m`.

For evaluating your solution, we will test it on the given problem data. Moreover, we will do suitable modifications of the parameters in `PhysicalConstants.m` and `SimulationConstants.m` and also test your estimator on those.

## Deliverables

Please hand in by e-mail your implementation of the particle filter in `Estimator.m`. Include the file into a zip-file, which you name `RFE10Ex2_Names.zip`, where *Names* is a list of the **pre- and surnames** of all students<sup>1</sup> who have worked on the solution (for example `RFE10Ex2_AngelaSchoellig_SebastianTrimpe.zip`).

Send your file to Angela ([aschoellig@ethz.ch](mailto:aschoellig@ethz.ch)) until the due date indicated above. We will send a confirmation e-mail upon receiving your solution. You are ultimately responsible that we receive your solution in time.

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<sup>1</sup>Up to three students are allowed to work together on the programming exercise. They will all receive the same grade.